

Fig. 5. Transmission factor *versus r/R* for case $\mu_0 = 0$, $2\theta = 90^\circ$.

Graphs like those in Figs. 4 and 5 allow optimum dimensions to be chosen for the target, from the standpoint of the transmission factor in diffraction studies. They also allow the value of the transmission factor to be found for non-tabulated α and β values, by an interpolation method.

Fig. 6 shows a plot of the transmission factor *versus* scattering angle for $\alpha = 0.4$ and for various values of the parameter β . The smallness of its variation with the scattering angle makes it easy to find, by interpolation, the values of the transmission factor for other scattering angles.

Fig. 6. Transmission factor *versus* scattering angle for case $\mu_{2}=0,~\mu_{1}R=0.4.$

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Ordering in Binary o Phases

BY F. J. SPOONER AND C. G. WILSON

Royal Military College of Science, Shrivenham, Swindon, Wiitshire, England

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An X-ray diffraction study has been made of the ordering of atoms in the following binary σ phases: NbOs, NbIr, NbRe, MoOs, MoIr and CrRe. Ordering of atoms among the different atomic sites has been shown to exist in all cases. From these results and others it is deduced that the size of the constituent atoms is a major factor in governing the filling of A , B , and D sites but in addition some valency electron factor governs the filling of C and E sites.

Introduction

Considerable work has been done in recent years on binary σ phases involving transition metals of all three long periods. Comprehensive surveys on the stability and composition of these phases have been carried out by Knapton (1958) and Greenfield & Beck (1956), but most of this work has been confined to phases involving elements in the first and second long periods. This report is concerned with an X-ray diffraction investigation of the order involved in additional σ phases consisting of elements of the second and third long periods: NbOs, NbIr, NbRe, MoOs, MoIr, WOs and in addition, a σ phase of particular interest: CrRe.

Table 1. Intensity data for σ phases

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 \ast Lines coincident with impurity phase.

Experimental

The preliminary work was done with X-ray powder photographs obtained with a 19 cm Debye-Scherrer camera and Ni-filtered Cu K_{α} radiation, the theoretical intensities being compared with those observed visually. More accurate results were obtained with an X-ray diffractometer and Cu Kx radiation obtained from a stabilized X-ray set and monochromatized by a bent quartz crystal. A proportional counter with single-channel pulse discrimination was used for detection and relative line intensities were obtained by measuring areas beneath the peaks on the recorder traces.

The presence of order was detected by the comparison of observed (diffractometer) and calculated line intensities. The detailed nature of the order was obtained by the method of trial and error, the final order scheme adopted being that which gave the best agreement between observed and calculated intensities. This method was very suitable because of the appreciable difference in scattering factors between the constituents of the σ phases chosen for the investigation (except σ -WOs). All calculated intensities were corrected for anomalous dispersion by means of the data given by Dauben & Templeton (1955). The atomic parameters used for these calculations are those determined by Bergman & Shoemaker (1954) for σ -FeCr. Since the results obtained are based mainly on low-angle lines, small inaccuracies in atomic parameters will have little effect on the results. The σ -WOs powder film provided an excellent reference film for the detection of order in other σ phases because of its similar cell size and the apparent random order displayed by virtue of the similarity of W and Os scattering factors. The agreement between observed and calculated intensities based on random order for this phase gives support for the wider use of the Bergman & Shoemaker parameters.

During the course of the investigation unit-cell sizes were determined from the Debye-Scherrer photographs with the use of the Nelson-Riley extrapolation method wherever possible; these measurements, together with the relevant intensity data for each sample, are given in Table 1. The order schemes used for the calculated intensities given in this table are included in the data given in Table 2. The normalization scheme chosen for the comparison of observed and calculated intensities was the summation of all intensity values excluding those which were associated with an impurity phase. A reliability index, $R = \sum (I_c - I_o)/\sum I_o$, was calculated for each σ phase, for both ordered and random schemes, again ignoring impurity lines, and is quoted in Table 1.

The final order schemes for CrRe and NbRe are excellent, the slightly higher value of R for NbRe being caused by the presence of the χ phase previously noted by Knapton. The σ phases NbOs, NbIr, MoOs, and MoIr have caused some difficulty owing to the appearance of the 210 reflexion which is very sensitive to order. It proved impossible to give this reflexion a higher calculated intensity consistent with a low value of R.

Some indication of the criterion for choosing a particular order scheme can be seen by examining the results in more detail, for example, the chosen order scheme for σ -MoIr having Ir atoms in 1A, 6.5D and $1E$ has a value for R of 0.117. The transfer of

Table 2. *Ordering schemes for* σ *phases*

(a) Kasper & Waterstrat (1956)

(b) Dickins, Douglas & Taylor (1956)

(c) Bergman & Shoemaker (1954)

(d) Wilson & Spooner (1963)

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(e) Decker, Waterstrat & Kasper (1954)

 (f) Forsyth & d'Alte da Veiga (1963)

 (q) Wilson (1963)

(h) Present work

one Ir atom from a D site to an A , B or C site results in values of R of 0.144 , 0.101 and 0.110 , respectively. and transfer of one atom from an E site to an A, B or C site results in values of R of 0.175, 0.144 and 0.120, respectively. These results suggest that the transfer of an Ir atom from a D site to a B site was desirable, but although the intensity agreement among the stronger reflexions is improved, the agreement among the low-angle lines is extremely poor. The adopted order schemes are those which gave as low a value of R as possible consistent with the requirement for good agreement with low angle lines and missing reflexions. As Wilson (1963) has pointed out for other σ phases, the presence of order is indicated by the missing and weak line intensities.

The validity of the chosen order schemes is also indicated to some extent by comparing the values of R with that for WOs, which is 0.109. Since this phase can be assumed to have random order because of the similarity in scattering factors for the constituent elements, there can be no improvement in the value of R.

Discussion

Order schemes which have been determined experimentally for various σ phases are given in Table 2. The elements constituting each σ phase are characterised as X or Y , where \overline{X} denotes an element to the left of manganese in the periodic table and Y an element to the right of manganese. Manganese and rhenium, which belong to the same group in the periodic table, are represented as Y-type elements. The Goldschmidt radius for coordination number 12 is given (in \AA) in brackets at the side of each element.

It was pointed out by Kasper & Waterstrat in 1954, that atoms of type Y generally occupy sites A and D which have the smallest coordination number (12) and smallest volume, atoms of type X generally occupy the site B which has the largest coordination number (15) and the largest volume, and sites C and E , which have the intermediate coordination number (14) and intermediate volume may be occupied by a mixture of X and Y atoms. This generalization applies to the order schemes proposed for the σ phases NbRe, NbOs, NbIr, MoOs and MoIr but not for σ -CrRe. The generalization suggests the importance of the chemical nature of the constituent atoms in a-phase order, but because of the characteristic variation of atomic size associated with the transition elements of each long period, the importance of the size effect in ordering becomes very apparent. The total number of valency electrons in s and d shells of the binary constituents (n_e) is also important in controlling order in some crystallographic sites as indicated below. For the σ phases listed in Table 2 the nature of the ordering associated with each crystallographic site may be summarized as follows:

- *Site A* $(0, 0, 0)$ $(CN 12)$: Occupied mainly by Y atoms except for σ -MoIr and σ -CrRe; $r_x > r_y$ except for σ -CrRe and σ -CrMn; independent of n_e .
- *Site B (x, x, 0: x*=0.3981) *(CN 15)*: Occupied mainly by X atoms except for σ -CrMn, σ -CrRe and σ -MoRe; $r_x < r_y$ for σ -CrMn and σ -CrRe.
- *Site C (x, y, 0: x=0.4632, y=0.1316) <i>(CN 14): Occu*pied by X and Y atoms but X atoms predominate except when $Y=Mn$ or Re; domination by X increases with n_e ; site equally divided when Y= Mn or Re.
- *Site D* $(x, y, 0: x=0.7376, y=0.0653)$ $(CN 12)$ *: Occu*pied mainly by Y atoms; $r_x > r_y$ except for σ -CrRe and σ -CrMn.
- *Site E* $(x, x, z: x=0.1823, z=0.2524)$ $(CN 14)$ *:* Occupied by X and Y atoms; Y atoms predominate for large *he.*

The fact that A and D sites are usually filled by ¥ atoms having smaller radii suggests the ordering requirements of size and chemical nature. Similar factors govern the filling of the large B sites. In particular, when the larger atom is Y-type as happens in σ -CrMn and σ -CrRe, the majority of B sites are filled by Y atoms. The size factor is not apparent in filling up the intermediate C and E sites, except for large values of *ne.* The phases containing Mn or Re are always distinguished by the mixed nature of the filling in C and E sites. A more detailed comparison of the exceptional phases CrMn, MoMn, MoRe and CrRe in which X and Y come from groups VI and VII of the periodic table shows that they have marked similarity in their ordering schemes. This aspect is much less apparent for σ phases whose atoms come from different groups of the periodic table.

The effect of an increasing valency electron contribution *per atom* can be estimated by considering the following series of σ phases:

- 1. $NbRe(6.1)$, $VFe(6.2)$, $NbOs(6.2)$, $NbIr(6.6)$, $VNi(7-1)$.
- 2. MoRe (6.55) , CrMn (6.75) , MoIr (6.85) , $MoFe(7.0), MoCo(7.2).$

In series 1 the X atom has five valency electrons and in series 2 it has six valency electrons, the average number of valency electrons per atom, of the unit cell being given in brackets. As the number of valency electrons per atom increases in each series the order approaches the simplest form in which Y atoms fill A and D sites only and X atoms fill B, C and E sites only.

The above results suggest that complex systematics, taking into account the size effect, the electronic factor and the chemical factor, govern the ordering in σ phases. The stability of the phase and its composition range would also seem to depend upon satisfying the ordering requirements since the only

 σ phases reported as being randomly ordered are σ -CrOs, σ -CrRe and σ -CrRu (Waterstrat & Kasper, 1957). The latter authors suggested random ordering for σ -CrRe but the results given above disprove this. So far the stability of the phase has been variously attributed to electronic effects (Sully, 1951; Bloom & Grant, 1953; Greenfield & Beck, 1954) and close-packing of spheres (Frank & Kasper, 1958; Stüwe, 1959). On the other hand, Haworth (1960) concludes that the occurrence of the σ phase cannot be predicted from normal intermediate phase considerations.

If the ordering requirements are an essential feature of this phase the random ordering reported in σ -CrOs and σ -CrRu requires an explanation. Since $r_{cr} = 1.28~\text{\AA}$ and $r_{0s}=1.34$ Å the Y atom Os is larger than the X atom Cr, so that the normal requirements (smaller atom and type Y) for filling A and D sites cannot be satisfied and in this respect the phase is similar to σ -CrRe examined above. Following the latter example, B sites would be filled by Y and X atoms, and, since the number of valency electrons per atom is only 6.6 for the composition used $(OsCr₂)$, it is expected that C and E sites would have mixed occupants. Thus, the presence of order might be difficult to detect and, in fact, Waterstrat & Kasper state that their measurements were not accurate enough to detect small amounts of ordering. Exactly similar arguments apply to σ -CrRu since Ru and Os belong to the same group of the periodic table.

From such considerations the general requirements for the stability of the σ phase formed by transition elements appear to be (i) a favourable atom size ratio $(r_x/r_y = 0.9-1.1$ in Table 2), (ii) the number of valency electrons per atom must lie within definite limits $(6.1-7.4$ in Table 2), and (iii) the elements X and Y must belong to the appropriate groups of the periodic table as defined above. These requirements are not satisfied when one of the binary elements is a non-transition element as in $\sigma\text{-Nb}_2\text{Al}$ (Forsyth, 1961) and σ -ZrRe (Tylkina, Povarova &

Savitskii, 1960) and other factors are required to explain the occurrence of the σ phase in these systems.

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